

**Relation b/w wave velocity (v)
Wavelength (y) & frequency (v)**

$$v = v\lambda$$

$$\text{Time period (T)} = \frac{1}{\text{Frequency}} = \frac{1}{v}$$

$$\text{Angular Frequency } (\omega) = 2\pi v$$

$$\text{Wave number, } v = \frac{1}{\text{wavelength}} = \frac{1}{\lambda}$$

Beats

Difference in frequencies of two superposing waves,

$$v_{\text{beat}} = v_1 \sim v_2$$

Displacement relation in a plane progressive wave

$$y(x, t) = A \sin(-kx + t)\omega$$

$$y(x, t) = A \sin 2\pi \left(\frac{t}{T} - \frac{x}{\lambda} \right)$$

Velocity amplitude $v_0 = A\omega^2$
Acceleration Amplitude $a_0 = A\omega^2$

Principle of superposition of waves

When two or more waves are propagating with different displacements then the net displacement of collective wave is given as $Y = y_1 + y_2 + y_3 + \dots + y_n$

Waves

Doppler Effect

General Formula,
Apparent Frequency

$$n' = n \left(\frac{v \pm v_o \pm v_s}{v \mp v_o \mp v_s} \right)$$

Here, v = speed of sound,
 v_o = observer speed
 v_s = source speed
 v_m = medium speed

Stationary Waves

Stationary waves

(i) In string: Fundamental Frequency, $v = \frac{1}{2l} \sqrt{\frac{T}{m}}$

(ii) In organ pipe:

(a) Open at both ends,

$$\text{Fundamental freq, or 1 harmonic } v = \frac{v}{2l}$$

(b) Closed at one end $v = \frac{v}{4l}$

(iii) • In open organ pipe, higher harmonics, both odd & even
• In closed organ pipe, higher harmonics, odd only.

Types

Matter Waves

Waves associated with particles like-electrons, protons, neutrons, atoms, molecules etc.

Mechanical Waves

Require material medium for their propagation

Electromagnetic Waves

Do not require any material medium for their propagation e.g., light waves

Transverse Waves

Individual particles of the medium oscillate perpendicular to the direction of propagation of wave

Longitudinal Waves

Individual particles of the medium oscillate along the direction of propagation of wave.

Properties

Essential properties for propagation
- Elasticity
- Inertia
- Minimum friction

Speed of transverse wave in a stretched string

$$V = \sqrt{\frac{T}{m}}, T = \text{tension} \& M = \text{mass/length}$$

Speed of a longitudinal wave speed of sound, $V = \sqrt{\frac{B}{\rho}}$

$$= \sqrt{\frac{\gamma}{\rho}} = \sqrt{\frac{P}{\rho}} = \sqrt{\frac{\gamma P}{\rho}} \text{ for air, } \gamma = 7/5$$